

Filler-gaps that neural networks fail to generalize

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Abstract

It can be difficult to separate abstract linguistic knowledge in recurrent neural networks (RNNs) from surface heuristics. In this work, we probe for highly abstract syntactic constraints that have been claimed to govern the behavior of filler-gap dependencies across different surface constructions. For models to generalize abstract patterns in expected ways to unseen data, they must share representational features in predictable ways. We use cumulative priming to test for representational overlap between disparate filler-gap constructions in English and find evidence that the models learn a general representation for the existence of filler-gap dependencies. However, we find no evidence that the models learn any of the shared underlying grammatical constraints we tested. Our work raises questions about the degree to which RNN language models learn abstract linguistic representations.

1 Introduction

While sentences appear highly variable on the surface, many syntactic constructions share the same underlying constraints, which determine their acceptability or grammaticality, i.e. the extent to which they are considered “well formed” through adherence to the rules of grammar. One of the strongest pieces of evidence for the existence of these shared underlying constraints are filler-gap constructions such as:

- (1) What does Leslie like ?

Filler-gap constructions contain a dependency between an overt filler (*what* in (1)) and a gap site (underlined above). The filler is bound to a referent (e.g., *Robin’s painting*) that can fill the gap:

- (2) Leslie likes Robin’s painting.

There are well-known restrictions (*islands*; Ross,

1967) that prevent certain words from participating in a filler-gap dependency. For example, it isn’t possible to form a filler-gap dependency with prenominal (left-branch) noun modifiers:¹

- (3) *Whose does Leslie like painting?

Further, very different filler-gap constructions obey shared underlying principles (e.g., *subjacency*; Chomsky, 1973). In this work, we probe recurrent neural network (RNN) language model understanding² of these underlying principles in English.

Recent work has claimed that recurrent neural network language models understand filler-gap dependencies (Chowdhury and Zamparelli, 2018; Wilcox et al., 2018, 2019). However, behavioral probing has suggested that this understanding is relatively superficial and doesn’t reflect the underlying constraints that govern filler-gap acceptability (Chaves, 2020). An intermediate possibility, which we explore in this paper, is that RNNs do acquire a basic understanding of the underlying constraints but that the learned representations of the constraints are too weak to correctly drive behavior in behavioral probing tasks.

We use cumulative priming (van Schijndel and Linzen, 2018; Prasad et al., 2019) to test for representational overlap between disparate constructions. While we find some evidence that RNNs learn a general representation for the existence of filler-gap dependencies (in keeping with Wilcox et al., 2018, 2019), we find no evidence that RNNs

¹Throughout this paper we adopt notational conventions from the syntax literature. * indicates an ungrammatical or unacceptable sentence, and ?? indicates a sentence whose acceptability is between wholly acceptable and wholly unacceptable.

²We use terms such as ‘understand’ and ‘represent’ to refer to the ability of RNN models to process language successfully. We do not mean to imply that models have true, deep understanding of linguistic phenomena as humans do. We simply use these terms for convenience.

learn shared representation of the associated governing constraints (in keeping with [Chaves, 2020](#)).

Several recent papers have highlighted ways in which RNN behavior actually reflects shallow surface heuristics ([McCoy et al., 2019](#); [Chaves, 2020](#); [Davis and van Schijndel, 2020](#)). Note that the representational overlap we seek in the present study is actually a requirement for appropriate generalization of abstract knowledge to unseen data. This is what differentiates abstract knowledge from the surface heuristics that make RNN behavior fragile to adversarial methods. Therefore, our finding that RNNs fail to learn any shared abstract constraints across filler-gap constructions despite being sensitive to the existence of filler-gap dependencies raises questions about the ability of these models to learn abstract generalizable linguistic patterns.

2 Background

There are a number of different kinds of filler-gap constructions whose behavior is governed by a variety of different underlying constraints (see [Table 1](#)). Previous work has probed model understanding of filler-gap dependencies by testing model performance on individual construction types rather than the underlying constraints that might govern them ([Chowdhury and Zamparelli, 2018](#); [Wilcox et al., 2018, 2019](#), c.f. [Chaves 2020](#)). These studies have followed the logic of the subject-verb agreement probing literature (e.g., [Linzen et al., 2016](#)): a model that understands filler-gap dependencies should assign greater probability to grammatical filler-gap dependencies than to ungrammatical filler-gap dependencies. However, certain properties are shared across a variety of filler-gap constructions, giving rise to the hypothesis in the syntax literature that there are shared constraints that underlie multiple different filler-gap constructions. [Chaves \(2020\)](#) identifies failure cases where neural language models incorrectly rank sentences containing acceptable and unacceptable filler-gap dependencies, possibly because they have overlearned the individual filler-gap constructions without understanding the broader underlying constraints. In this paper, we test whether models understand four underlying filler-gap constraints that have been widely studied in the syntax literature. Specifically, we test whether multiple constructions that are governed by a single constraint share any representational features that are not present in other constructions. If such selec-

tive representational overlap exists, it could be an indication that the models do understand the underlying constraints but that their representation is too weak to correctly rank acceptable/unacceptable sentence pairs.

Cumulative priming has been introduced as a method for probing the linguistic representations encoded in RNNs ([van Schijndel and Linzen, 2018](#); [Prasad et al., 2019](#); [Lepori et al., 2020](#)).³ This approach involves fine-tuning pretrained models for a single epoch with a small amount of additional training data. The pretrained model acts as a filter on the linguistic features learned during fine-tuning. More salient features will be affected by the fine-tuning to a larger degree than less salient features. By measuring the responsiveness of the model to linguistic input before and after priming (fine-tuning), researchers can identify which linguistic features are salient for the pretrained model. Importantly, if one construction primes a different construction, there is representational overlap between the two constructions within the model. Therefore, this approach provides a direct method of separating abstract linguistic knowledge from surface heuristics.

3 Constructions

We analyze eight types of syntactic constructions involving filler-gap dependencies in English. Syntacticians often refer to these dependencies as extractions, which alludes to the linguistic theory that filler phrases originate at the gap site before being *extracted* to the filler site during language production.

3.1 Adjunct islands

An adjunct island is formed from an adjunct clause, out of which *wh*-extraction is not possible. Adjunct clauses are introduced by *because*, *if*, and *when*, as well as by relative clauses.

- (4) a. She ate her hat because they announced the plan.
b. ***What** did she eat her hat because they announced ?

³For example, [Prasad et al. \(2019\)](#) use cumulative priming to show that RNN language models cluster multiple different kinds of relative clauses together in representation space (suggesting an abstract relative clause representation), and that simple syntactic features (passivity, relative clause reduction) are similarly clustered. However, the syntactic abstractions probed by [Prasad et al. \(2019\)](#) are still tied to surface cues.

Construction	Examples	L	S	E	D
Adjunct island	*What did you go home because you needed to do __?	-	-	-	
Wh- island	*Whom did Susan ask why Sam was waiting for __?		-	-	(+)
Subject island	*Who is that __ went home likely?	-	-	-	
Left branch island	*Whose does Susan like __ account?		-	-	(+)
Coordinate structure island	*What did Sam eat __ and broccoli?			+	
Complex NP island	*What did you hear the claim that Fred solved __?		-	-	
Object extraction	Who is it probable that Bill likes __?	+		+	(+)
Non-bridge verb island	*How did she whisper that he had died __?	?	?		

Table 1: Island constructions (rows) and the associated underlying constraints (L-marking, Subjacency, and the Empty Category Principle) that govern their behavior. We only examine constraints that are hypothesized to apply to multiple of our construction types. For constraints that are thought to be particularly influential of a construction, we denote the influence with +/- . For example, subject island extractions are unacceptable because they violate L-marking, while object extractions are acceptable because they adhere to L-marking. Discourse-Linking (D-linking) is an optional shared feature that can make some unacceptable constructions more acceptable.

3.2 Wh-islands

A wh-island is created by an embedded sentence which is introduced by a wh-word. Extraction out of a wh-island results in an unacceptable sentence.

- (5) a. Sam wonders who solved the problem.
b. ***What** does Sam wonder who solved __?

3.3 Subject islands

A subject island is formed from a subject clause or a subject phrase, out of which wh-movement is not possible.

- (6) a. That he has met Julia Roberts is unlikely.
b. ***Who** is that __ has met Julia Roberts unlikely?
(7) a. The rumour about Susan was circulating.
b. ***Whom** was the rumour about __ circulating?

3.4 Left branch islands

Left branch islands consist of noun phrases with modifiers, such as possessive determiners and attributive adjectives, that appear on a left branch under the noun. These preceding modifiers of a noun cannot be extracted from a noun phrase.

- (8) a. Eric likes John's boat.
b. ***Whose** does Eric like __ boat?
(9) a. You failed the difficult test.

- b. ***How difficult** did you fail the __ test?

3.5 Coordinate structure islands

Coordinate structure islands allow extraction out of a conjunct of a coordinate structure only if the extraction affects all the conjuncts of the coordinate structure equally, i.e. if the extraction occurs across the board.

- (10) a. They ordered [tiramisu] and [espresso].
b. ***What** did they order [tiramisu] and __?
c. ***What** did they order __ and [espresso]?
(11) a. Alicia [gave a guitar to me] and [loaned a trumpet to you].
b. **What** did Alicia [give __ to me] and [loan __ to you]?

3.6 Complex noun phrase islands

Complex noun phrase islands ban extraction from the clausal complement of a noun, and from a relative clause modifying a noun.

- (12) a. You heard the rumour that Bill speaks a Balkan language.
b. ***What** did you hear the rumour that Bill speaks __?
(13) a. They hired someone who cleans a dirty surface.
b. ***What dirty surface** did they hire someone who cleans __?

3.7 Object extraction

Object extraction is when a filler-gap dependency involves an object clause or phrase. In contrast to subject islands, object extraction produces acceptable sentences.

- (14) a. She told me that her mother is a teacher.
b. **Her mother**, she told me __, is a teacher.
- (15) a. It is important to invite Will to our party.
b. **Who** is it important to invite __ to our party?

3.8 Non-bridge verb islands

Non-bridge verb islands ban extraction out of that-clause verb complements when the matrix verb is a non-bridge verb. Non-bridge verbs include manner-of-speaking verbs, such as whisper or shout.

- (16) a. She thinks that he died in his sleep.
b. **How** does she think that he died __?
- (17) a. She whispered that he had died in his sleep.
b. ***How** did she whisper that he had died __?

The unacceptability of non-bridge verb islands hinges on the frequency of the verb (Liu et al., 2019). Therefore, the degree to which different constraints govern its behavior is hotly debated. As such, we do not use this construction when probing for underlying constraint knowledge. However, we do include grammatical variants of this construction (16-b) as acceptable stimuli in our general filler-gap analysis (Section 7.2).

4 Constraints

We analyze four underlying syntactic principles that have been hypothesized to govern the behavior of the above constructions.

4.1 Subjacency

Subjacency (Chomsky, 1973) is defined in terms of the notion of extraction mentioned in the previous section. Syntacticians theorize that a filler is iteratively extracted from its gap site to particular possible landing sites during language production. The subjacency principle states that extraction is only permitted if all landing site positions that intervene

between the filler and the gap are unfilled during the extraction process. If the possible structural positions are unavailable because they are filled with another lexical item, extraction is blocked and the resulting filler-gap dependency is deemed ungrammatical. The effect of the subjacency constraint can be observed in the above examples of Wh-islands, subject islands, left branch islands, and complex noun phrase islands.

4.2 Empty Category Principle

The Empty Category Principle (ECP; Kayne, 1980; Chomsky, 1981) is a syntactic constraint that requires a gap be properly governed. To be properly governed, gaps must be identifiable as empty positions in the surface structure of a sentence, which allows a tree structure to “remember” what has happened at earlier stages of a sentence’s derivation. Adherence to this constraint makes extraction of a wh-word from a subject or adjunct position ungrammatical, while extraction from an object position or from a coordinate structure island is grammatical.

4.3 L-marking

L-Marking (Chomsky, 1986) is a process that defines the types of categories that act as barriers to movement, including extraction. A category is L-marked if and only if it gets its theta role from a lexical head. A theta role specifies the number and type of arguments that are syntactically required by a particular verb. For example, direct objects in English receive theta roles from the main verb, while adjuncts and subjects do not. Movement is grammatical only when it occurs out of an L-marked phrase, as in object extraction but not in adjunct or subject islands.

4.4 D-linking

Discourse-linking or D-linking (Pesetsky, 1987) indicates that there is a pre-existing contextual relationship between a filler and its associated noun phrase (e.g., *which man*). D-linked phrases contrast with non-discourse linked interrogative pronouns such as *who*, which do not necessarily imply familiar discourse entities. Left branch island extractions and wh-island extractions become more acceptable with a D-linked wh-phrase (Pesetsky, 1987; Atkinson et al., 2015). For example:

- (18) a. ??**Which book** did Will ask why John read __?

- b. ***What** did Will ask why John read ___?

Since D-linking is an optional feature that can be added to filler-gap constructions, it isn't something that can be violated, per se. Therefore, in our analyses to probe for D-linking knowledge we only test constructions that adhere to D-linking (18-a).

5 Models

We focused in this work on recurrent neural language models with long short-term memory units (LSTMs; Hochreiter and Schmidhuber, 1997). We analyzed five of the highest performing models released by van Schijndel et al. (2019),⁴ who showed that these models perform comparably to state-of-the-art transformers GPT and BERT on many simple syntactic agreement tasks. The models are 2-layer LSTMs with 400 hidden units per layer, each with a unique random initialization, trained on 80 million training tokens of English Wikipedia data. Analyzing multiple similar models with different random seeds helps ensure that our results are more representative of a class of models rather than simply revealing how a single exceptional model behaves (e.g., BERT; Devlin et al., 2019). This is very important given the speed with which new individual models supplant each other in the literature. Our results are averaged across all five of our models.

6 Method

We generated 40 sentences per construction type, partitioned into a prime set (15 sentences) and a test set (25 sentences). Sentences are available in the supplementary materials.

We measured model performance as the average surprisal (negative log-probability; Shannon, 1948; Hale, 2001) experienced by a model M when processing each word w_i of each sentence s_j in a set S :

$$\text{perf}(M, S) = -\frac{1}{|S|} \sum_{j=1}^{|S|} \frac{1}{|s_j|} \sum_{i=1}^{|s_j|} \log P_M(w_i | w_{0..i-1}) \quad (1)$$

Priming is achieved by giving the model a single training epoch on the set of priming stimuli

S_P . This process produces a modified model M'_P whose performance on a test set S_T differs from the original model in a way that gives insight into the representations of the original model. One way to think about this is that pretraining provides a certain kind of model initialization. Priming the model moves the model representations along gradients which are characterized by an interaction of the priming stimuli and the initial pre-trained model state. If a set of priming stimuli has a consistent set of features, the initial state's sensitivity to that set of features can be probed with those stimuli. Following Prasad et al. (2019), we denote this raw effect of priming (also known as adaptation) as:

$$\mathbb{A}(S_T | S_P, M) = \text{perf}(M, S_T) - \text{perf}(M'_P, S_T) \quad (2)$$

We are actually interested in the interaction between the original model and the priming set, but the above measure also includes the interaction between the original model and the test set. Less expected (more surprising) test constructions can produce larger measures of priming simply because the original model has more room for improvement (Prasad et al., 2019). Therefore, we used linear regression to predict the size of the priming effect using the original model's performance on the test set:

$$\mathbb{A}(S_T | S_P, M) \sim \beta_0 + \beta_1 \text{perf}(M, S_T) + \epsilon \quad (3)$$

To obtain a more appropriate *adaptation effect* (AE) for analysis, we subtracted out the predicted linear relation between the original model's test performance and the size of the final priming effect:

$$AE(S_T | S_P, M) = \mathbb{A}(S_T | S_P, M) - \beta_1 \text{perf}(M, S_T) \quad (4)$$

This measure of priming more directly reflects the interaction of the original model with the priming set, normalizing the adaptation effect by each model and prime construction, and producing a comparable measure to that studied by Prasad et al. (2019). Across all analyses, greater values of the adaptation effect indicate greater similarity between adaptation and test structures.

Recently, Kodner and Gupta (2020) have raised concerns about the efficacy of this technique in

⁴<https://zenodo.org/record/3559340>

probing model representations. Specifically, they showed that non-syntactic models can produce qualitative patterns that appear to mimic the effects of syntactic priming. However, their results demonstrate that while the qualitative patterns may be similar, syntactic priming produces much larger effects in syntactic models compared with non-syntactic models. Therefore, their results should not be taken as an indictment of this methodology but simply that reasonable baselines must be employed when using this probing method.

7 Probing for Filler-Gaps

7.1 Null-Prime Baseline

Adaptation effects are difficult to interpret on their own. A positive effect indicates that priming produced more accurate predictions in a given class, while a negative effect indicates the opposite, but the magnitude of the effect is tricky to interpret. Following Prasad et al. (2019), for each analysis we define a class of interest and then compare within-class adaptation effects to cross-class adaptation effects. However, as Kodner and Gupta (2020) point out, spurious correlations may be introduced during stimulus creation/selection. Therefore, we also compare to null-primed models, which use the same original models but we prime them on prime sets whose sentences are shuffled at the word level (as Example (19-b)):

- (19) a. ***What** does Sam wonder who solved ___?
 b. *Sam wonder What does solved who?

These shuffled null-prime stimuli do not contain any filler-gap dependencies, and so the adaptation effect from null-priming must represent phenomena in which we are not interested (e.g., lexical priming). Our effect-of-interest (filler-gap knowledge) is therefore reflected in any adaptation effect in excess of the null-prime effect.

7.2 Priming Filler-Gap Existence

First we ask whether the models have learned to represent the overall existence of a filler-gap dependency. To test this, we partition our stimuli into wholly acceptable constructions (involving object extraction, bridge verb extraction, and instances of left branch extraction and coordinate structure extraction) and wholly unacceptable constructions (the remaining constructions). We then test whether

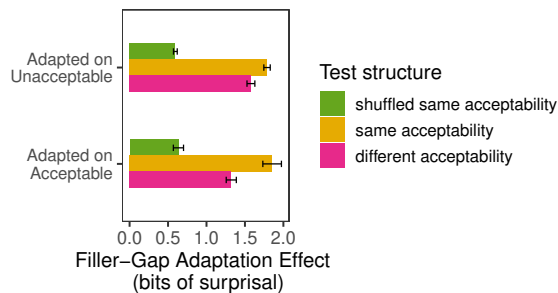


Figure 1: Adaptation effect produced by the existence of a filler-gap dependency. The green bars (top) represent priming a construction type from shuffled instances of similar acceptability. The gold bars (middle) represent the grammatical priming grammatical and ungrammatical priming ungrammatical effect. The pink bars (bottom) represent the acceptable priming unacceptable and vice versa effects.

grammatical constructions can prime ungrammatical constructions and vice versa.

Although at the sentence level, ungrammatical constructions do not have a resolvable filler-gap dependency, that unacceptability only manifests at or near the end of the sentence. From the perspective of our unidirectional models, both sets of sentences initially require the retention of an apparent “filler.” We therefore hypothesize that if the models understand filler-gap, both of these sets should initially contain a shared unidirectional representation of filler-gap existence.

We find that grammatical constructions prime ungrammatical constructions beyond the baseline shuffled adaptation effect (Figure 1). In other words, fine-tuning on grammatical items teaches the models how to process ungrammatical items with apparent filler-gap dependencies. We also find that ungrammatical items prime grammatical items in a similar fashion. Since the single unifying feature present in both grammatical and ungrammatical constructions is the presence of an apparent filler-gap dependency, these results suggest that the models contain a representation of filler-gap existence that is shared across constructions.

8 Probing for Filler-Gap Constraints

We next consider constraint-specific priming in order to determine whether the aforementioned abstraction of filler-gap dependency has shared substructure that would indicate understanding of the filler-gap constraints described in Section 4.

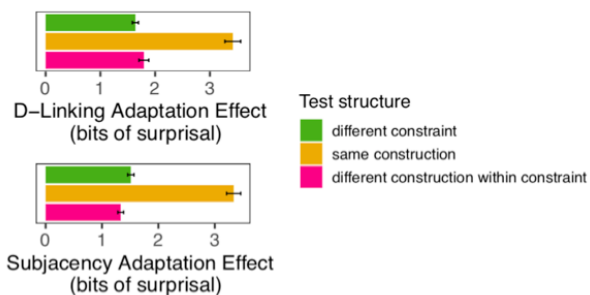


Figure 2: Adaptation effect due to D-linking adherence and Subjacency violation. Green bars (top) represent priming of a construction with constructions from other constraints (indicating general filler-gap priming). Gold bars (middle) represent priming of each construction with other constructions of the same type. Pink bars (bottom) represent priming of each construction with other constructions governed by the same constraint.

8.1 Filler-Gap Existence Baseline

In the previous section, we found that RNNs represent the existence of filler-gap dependencies similarly across construction types. We are therefore interested in whether the models systematically differentiate between filler-gap constructions that are governed by different constraints. If so, we would expect the shared representation of a constraint to produce greater priming within a constraint than across constraints. Therefore, rather than using shuffled sentences, our lower-bound baseline in this section consists of the adaptation effect from priming on sentences that do not share a constraint (green bars). We also use an upper-bound baseline adaptation effect from when models are tested and primed with the same syntactic construction (though the actual sentences differed; gold bars).

8.2 Priming Filler-Gap Constraints

Our results are presented in Figures 2 and 3. We divided our constructions based on those that consistently adhere to or violate particular constraints. If an abstract filler-gap constraint is learned by the model, then constraint adherence should prime adherence in the test set and constraint violation should prime violation in the test set (pink bars). Further, true understanding of a constraint would mean that constraint adherence would prime subsequent adherence more than subsequent violation and vice versa (purple bars reflect adherence priming violation and vice versa).

For subjacency, simple existence of filler-gap

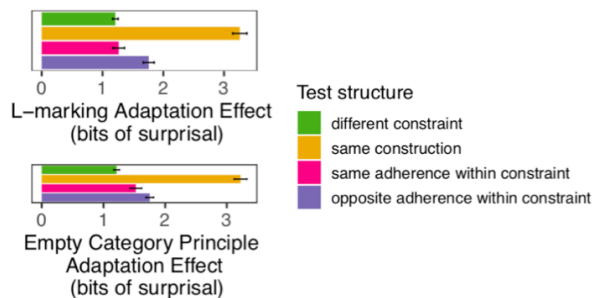


Figure 3: Adaptation effect due to L-marking and ECP. Some constructions adhered to these constraints and others violated them. Green bars (top) represent priming of a construction with constructions from other constraints (indicating general filler-gap priming). Gold bars (second from top) represent priming of each construction with other constructions of the same type. Pink bars (third from top) represent adherence priming adherence and violation priming violation. Purple bars (bottom) represent adherence priming violation and vice versa.

primed the model significantly more than other constructions involving subjacency.⁵ Adherence to D-linking primed subsequent adherence to D-linking significantly more than simple filler-gap existence did, suggesting that perhaps the models do have an abstract representation of D-linking (but see Section 8.3).

Constructions involving L-marking and ECP produced significantly more priming in the mismatched adherence condition (adherence priming violation; violation priming adherence) than the matched adherence condition (adherence priming adherence; violation priming violation), suggesting that these constraints aren't learned by RNN language models. In fact, matched adherence in L-marking was not significantly different than priming with unrelated filler-gap sentences. Matched adherence in ECP did produce significantly greater priming than filler-gap existence, but since the priming effect was even greater for mismatched adherence, we can conclude that the model did not have an abstract representation of ECP that modulates filler-gap acceptability in a predictable way.

8.3 D-Linking Modulation

Our priming results in the previous subsection suggested that D-linked stimuli prime subsequent D-linking more than simple filler-gap existence does. However, D-linking also has an explicit surface

⁵Significance was determined by two-sample t-tests. See Supplementary Materials for details.

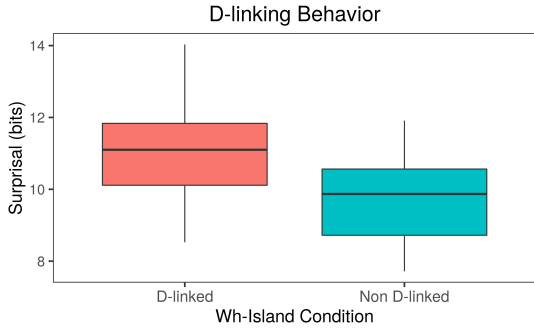


Figure 4: Pretrained model surprisal of D-linked wh-extractions (left) and non-D-linked wh-extractions (right). If the models learned to use D-linking to modulate the acceptability of filler-gap constructions, the surprisal of D-linked constructions should be lower.

cue, sentence-initial ‘which’, that could produce representational clustering even without an abstract linguistic concept of the constraint. Therefore, in this section, we use a behavioral probe to determine whether the models actually encode the underlying constraint.

As noted above, D-linking increases the acceptability of a filler-gap dependency.

- (20) a. ??**Which** book did Will ask why John read __?
- b. ***What** did Will ask why John read __?

At the filler, D-linking provides semantic clues to help predict the gap site (e.g., books will be bought or read but not eaten), and at the gap site D-linking greatly reduces the set of possible referents and eases retrieval of the correct referent both for syntactic attachment of the filler and for comprehension of the sentence (e.g., John did not read a sign or a scroll). We therefore expect that a model that understands D-linking will find D-linked sentences easier to process, similar to humans. We compared model performance (average surprisal; Equation 1) on each set of constructions. If a model uses D-linking in a human-like way, the D-linked sentences (like (20-a)) should produce better performance (be less surprising) than the non-D-linked sentences (like (20-b)).

In contrast to humans, RNNs find D-linked sentences more surprising than non-D-linked ones (Figure 4). In other words, the models prefer the less acceptable filler-gap constructions. These results suggest that the underlying D-linking feature

is not learned even in a construction-specific way, let alone in a way that is shared across multiple constructions.

Based on the findings in the current and preceding sections, we conclude that RNN language models do not go beyond representing the existence of filler-gap dependencies to representing any of the shared underlying constraints we studied here.

9 Discussion

Our results support previous behavioral findings that recurrent neural language models acquire some abstract concept of “filler-gap dependency” (Chowdhury and Zamparelli, 2018; Wilcox et al., 2018, 2019), but go farther than those findings by indicating that this concept is representationally shared across different constructions. However, our findings also indicate that RNNs do not encode any of the syntactic filler-gap constraints we studied.

Both grammatical and ungrammatical sentences involving apparent filler-gap dependencies cause models to anticipate the existence of subsequent filler-gap dependencies. However, in two of four cases, the baseline adaptation effect from priming on unrelated filler-gap constructions was comparable to or greater than that from priming on other constructions governed by the same constraint. Constructions that violated ECP and L-marking were represented similarly to constructions that adhered to those same constraints. And models assigned lower probability to sentences involving D-linking than sentences without D-linking, which is the opposite of human results.

Overall, our results provide robust evidence that Chaves (2020) was correct that recurrent neural language models do not fully understand filler-gap constructions. While it is entirely possible that the constraints analyzed in this work do not actually govern filler-gap dependencies (i.e. these particular syntactic theories may be incorrect), we chose four constraints that have been very widely studied by syntacticians precisely because of their broad coverage. Therefore, even if the underlying syntactic theories are incorrect, it is conceivable that RNNs could induce these constraints as plausible abstractions to aid in filler-gap processing. It is therefore striking that RNNs learn none of them.

One might wonder whether our priming sets simply needed to be larger to observe the desired priming effects. Our priming sets consisted of 15 items, which is comparable to the number of priming stim-

uli used by Prasad et al. (2019) and Kodner and Gupta (2020). Since the constraints we study involve fewer surface cues, they could require more priming data to produce noticeable effects. However, our non-baseline adaptation effects were around 1.5 bits, which is much larger than the 0.5-1 bit priming effects seen in those previous studies. Since we are already seeing large priming effects with these constructions, it seems unlikely that increasing the amount of priming data would produce qualitatively different effects.

We selected four common, well-studied filler-gap influences from the syntax literature and tested whether RNNs shared representational features across filler-gap constructions in a way that would suggest they had learned those constraints. While we did find evidence that RNNs encode some general representation of the existence of filler-gap dependencies, we found no evidence for more abstract underlying shared constraints. That is, while we find that RNN language models can learn abstract representations that are shared across constructions, our work raises questions about the depth of such abstractions.

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A Supplementary Material

A.1 Adjunct island stimuli

A.1.1 Adaptation set

- *What did he hear that I hired someone because a rumour has been?
- *What did she go to buy a gift because she is?
- *What did they not like that you were a teacher when they heard about you?
- *Where did they scold me when I went?
- *What did you go home because you needed to do?
- *What does Alex like the woman who wears?
- *Which topic did you leave because Mary talked about?
- *What will I eat my hat if John buys?
- *What will I buy a cup of coffee when I get?
- *What have they been circulating because she wears?
- *What did she say that I was waiting for someone who might get for Christmas?
- *What did they not like that I am likely to go because you are?
- *What did he hear that they gave a guitar to him when you gave to me?
- *What does he speak a Balkan language because I speak?
- *What did he hear that they solved the second problem because she read?

A.1.2 Test set

- *What did I buy a guitar for myself because they heard?
- *What will they fail the test if they do not?
- *Whom will he hire someone if I need?
- *What has he been circulating who he thought was?
- *What will he try to call you if she buys?
- *What did she say she would like the man if he read?
- *Where did I buy a coffee for myself because I went?
- *What will he circulate a call if she buys?
- *Whom did she say that she gave a guitar to me when I hired?
- *What did he get a new phone for Christmas because she saw?
- *What did you need to do that if you were to go and buy?
- *What did she eat the broccoli because they announced?
- *Where did she say that he will hear a rumour if she is?
- *What does he speak a Balkan language because

you were?

- *Who did she say that she wears extravagant rings when she is waiting for?
- *What does Jim eat a yellow candy whenever Pam watches?
- *Whom did the pregnant teddy bear assert that Julia Roberts came because Susan hired?
- *What did Eric solve problems by Fourier analysis because Will loaned him?
- *What did Elnar dance a ballet when the pretty agent stole?
- *What will I eat scandalous broccoli if the extravagant woman sings?
- *What will the blue brothers date Susan and direct the crafty movie if he gets?
- *What does Julia Roberts like the discreet agent who robbed?
- *Where did Sam announce a party boat when I went?
- *Where did Jim quip that the pretty window was silly when Susan arrived?
- *What will Fred wait for a homework if he sings?

A.2 Wh island stimuli

A.2.1 Adaptation set

- ??What does John wonder where Eric went to buy?
- *Whom did Susan ask why Sam was waiting for?
- *What did they not like that Will asked how Sam speaks?
- *What did Will ask why John read?
- *Who did he hear that Eric asked where Sam is waiting for?
- *Whom did Sam ask what Elnar told?
- *How did they forget which problem they should solve?
- *What did Sam wonder who solved?
- *What did I forget who directed that I saw yesterday?
- *Where did he hear that my sister asked which direction to take for?
- *What does Sam wonder why Will buys?
- *What did he hear that Sam asked when Alexa directed that I saw yesterday?
- *What did Fred think how Eric is likely to do?
- *Whom did they not like that Fred wondered why Elnar hired?
- *What did Sam wonder what Elnar has been?

A.2.2 Test set

- *Where did Alex ask who Elnar took?
- *What did she say that John asked who will read?
- *Where did Elnar ask how John went?

- *What did Will ask why Alex wears?
- *What did she say that Will thinks he knows where Sam announced?
- *What did they not like that Elnar wonders how Alex was?
- *What did Alex ask when Eric ate?
- *What does Sam wonder where Susan buys?
- *What does Will wonder how he will read?
- *How did he hear that Sam thinks he knows where Elnar gets?
- *Whom does Eric wonder how Susan is waiting for?
- *What did Alex ask why Susan is?
- *What did Elnar ask who Will is for?
- *Whom did Fred ask where Sam loaned a trumpet to?
- *What did he hear that Sam asked who Eric heard about?
- *What did Jim ask why a discreet rumour was?
- *What does Pam wonder when the blue homework will eat?
- *Where did Julia Roberts ask who took the expensive picture to?
- *How did she hear that Elnar thinks he hires where Julia Roberts buys?
- *Whom did the expensive experience ask what the lucky teddy bear told?
- *What did the English essays ask when the probable account made?
- *What did the espresso wonder who announced?
- *What did the party think how the boat is unrealistic to do?
- *What did the brothers ask why the crafty story plays?
- *Where did the scandalous girls ask how the salad went?

A.3 Subject island stimuli

A.3.1 Adaptation set

- *Who is that went home likely?
- ??Whom was the story about funny?
- *What has a rumor that you read been circulating?
- *What was the account about difficult?
- *Who is that announced a plan possible?
- *Who is that speaks a Balkan language funny?
- *What was about her difficult?
- *Who is that he has met unlikely?
- *Whom did someone who knows meet them?
- *What was that would be made unrealistic?
- *Who was that directed the movie that I saw yesterday claimed by Susan?

- *Whom did one story about buy a cup of coffee?
- *What was that they announced about speaking a Balkan language?
- *Whom were the books about waiting for someone?
- *What does that John wears make the plan difficult?

A.3.2 Test set

- *Who was that quipped about Fourier Analysis funny?
- *Whom were two rumours about waiting?
- *Who does that wears extravagant rings make the plan unrealistic?
- *Whom loaned that Fred heard the claim a trumpet to you?
- *Who is that is a teacher unlikely?
- *Whom does one story about claim the possibility is unrealistic?
- *What was that she likely heard true?
- *Who was that knows someone probable?
- *Who does that got a new phone for Christmas not make sense?
- *Whom did an account for buy a gift?
- *What is that come to our party likely?
- *Who does the extravagant rings that takes to school are funny?
- *Who is that Elnar is trying to call unrealistic?
- *Who was that they loaned a trumpet to funny?
- *Who was that heard the claim funny?
- *Who is that went to the discreet candy store expensive?
- *Whom was the lucky party about circulating?
- *What is that John is scandalous?
- *What were two pregnant girls from dating?
- *Whom was one claim about funny to Julia Roberts?
- *What was that they robbed an experience?
- *Who was that they loaned a lucky guitar to unrealistic?
- *What was the blue window that announced was crafty?
- *What does one agent of like the aria?
- *What was that Mary ate difficult for you?

A.4 Object island stimuli

A.4.1 Adaptation set

- Whom did he tell that his mother is a teacher?
- Who is it important to invite to our party?
- Who is it probable that Bill likes?
- Which book did John hear a rumor that you had read?

Which car did John announce a plan to fix?
 Who does he like that their boat hired?
 Who is it important that Eric call about?
 Who did he hear that it is important to invite?
 Whom did she say that it is probable Alex saw?
 What is it important that Fred ate?
 What did they not like that Eric claimed that his story is?
 Which experience did Susan write a story to share?
 What do you hate that their story buys?
 What did she say that Eric thinks that their cat wears?
 Who is it important to call to our party?

A.4.2 Test set

Who did he hear that it is important to see?
 What is it important that John buys?
 Who did he hear that it is important that Fred knows?
 Where did Alex tell you that she went?
 What did he hear that Sam does not do?
 What did he hear that Alex thinks their car needed to do?
 Who is it probable that Alex helped?
 What did they not like that you read that Susan is trying to give you?
 Who did they not like that it is probable that Sam met?
 Who is it probable that the account is waiting for?
 Who did they not like that it is important to fix?
 Who did they not like that it is probable that Susan called?
 What did Alex buy you?
 What did she say that John thinks that their rumour was?
 What is it important that Sam eats for Christmas?
 Who is it scandalous that the silly candy store is demanding for?
 Who did they quip that it is expensive to date?
 What did they not like that it is circulating that Fourier analysis solved?
 What does Alex not whisper that you robbed?
 Where is it unrealistic that Pam goes to for Christmas?
 What did he hear that it is extravagant to claim?
 What is it likely that the teacher buys?
 What did he hear that it is funny that a cup of coffee solves?
 Who did the book tell me went to the expensive store?
 Who did the TV experience assert watched a ballet on Broadway?

A.5 Left branch island stimuli

A.5.1 Adaptation set

*Whose does Susan like account?
 *How expensive did he buy a boat?
 *Whose does Eric like boat?
 *How yellow did they not like that Eric loaned a trumpet?
 *How silly did they not like that he told me?
 *How good did he hear that is she a teacher?
 *Whose did she buy book?
 *Which (man's) did you see picture?
 *How large did Alex eat a salad for lunch?
 *Whose does my sister like shows?
 ??How good does Elnar like possibilities?
 ??How fair is Sam a teacher?
 *How pretty did she say that you are waiting for a woman?
 *How second did John solve the problem?
 ??How new did she say that Will went to buy a gift?

A.5.2 Test set

*How crafty did she say that he directed the movie that I saw yesterday?
 ??How discreet did Susan hire an agent?
 ??How pretty does Susan like the woman?
 *How difficult did he hear that you failed the test?
 *Whose did she say that John eats hat?
 ??How crafty did she say that he announced a plan?
 ??How pretty did he hear that she read the Sandman comics?
 *What kind does Susan speak a language?
 *How expensive did they not like that she wears rings?
 *How pretty did she say that Susan likes the woman?
 *How blue did he hear that Eric loaned a trumpet to you?
 *How extravagant did they not like that Will wears rings?
 *Whose did they not like that I ate old hat?
 *How scandalous did he hear that Eric heard a rumour?
 ??How blue did Alex give a guitar to me?
 *How circulating did she hear that he buys candy stores?
 *How crafty did Julia Roberts not demand that I hire a teddy bear?
 *How difficult does the blue agent do math homework?
 *How important is she dating the broccoli brothers?

??How unrealistic is the funny man singing an aria?
*How discreet does the TV wonder why he hired a tiramisu?
*How silly did the lucky girls ask how she found a boat on the way to Broadway?
??How large did Julia Roberts invite a party to the city?
??How likely did he announce a plan to buy a bean?
??How important does the TV experience like the possibility?

A.6 Coordinate structure island stimuli

A.6.1 Adaptation set

*What does Alex like and beans?
*What did they not like that Fred likes cars and?
*What did Sam eat beans and?
What did Sam give to me and loan to you?
Whom is he waiting for and trying to call?
What did my sister hear that Susan danced for me and sang for you?
Who did they say that Sam helped and took care of?
*Which beverage did they order tiramisu and?
*Which dessert did he hear that they ordered and espresso?
Which tasks did she say that he has in math and in English?
What did I buy for him and take for him?
*What did Will whisper or car?
*What did she say that Sam whispered rumour and?
*What did Elnar buy and boats?
*What did you not study or?

A.6.2 Test set

*What did they not like that John likes and accounts?
Who did she hear a rumour about and wait for?
*What did he hear that Eric ate accounts and? What did Will buy?
What things did you read about and announce about?
*What did he announce a plan and speak?
Which subjects did she not study for or fail the test for?
What did Sam order for me and borrow for you?
*What does Will like and girls?
*What did they not like that Will bought tiramisu and?
*What did he hear that Elnar ate and story?
Which things did she solve and give?
*What did he announce a plan and solve by?
*What does Susan like and mothers?

What did she hear about me and take about you?
*What did Julia Roberts demand the scandalous rumour and whisper?
*What does the unrealistic brother like and silly parties?
*What does the crafty possibility eat probable windows and?
*What does the directed candy store like circulating salads and?
*What did the expensive Fourier analysis not like that the difficult study bought and discreet ballet?
*What did he rob a silly possibility and date?
*What does the lucky street hire and accounts?
What did the pretty experience assert for me and hire for you?
What did the extravagant cup of coffee quip for me and solve for you?
*What does the Balkan language like Christmas and?

A.7 Complex noun phrase island stimuli

A.7.1 Adaptation set

*What did you hear the claim that Fred solved?
*What does she like the possibility that she might get for Christmas?
*What Balkan language did they hire someone who speaks?
*What candy store did they meet someone who robbed yesterday?
*Which direction did you see a sign that Susan pointed us in?
*What did we hear a rumour that Sam thinks?
*How many cities does Bill have brothers who live in?
*What does Frank believe the rumour that Susan sleeps with?
*Who don't I believe the claim that Jim likes?
*Who did my sister say that Alex is the only person who knows?
*How does she believe that Eric solves?
*What did we hear the claim that Will thinks that he will buy?
*What subjects does Susan have students who failed tests in?
*What don't they believe the claim that Elnar speaks?
*What did my sister hear that Susan likes?

A.8 Test set

*Who don't we believe the rumour that Sam is dating?

*How does Will think that she is dating someone who solves?

*What does she believe the rumour that she might have this year?

*How many cities does he know brothers who live in?

*Who do they believe the claim that he likes?

*What did she hear a rumour that Susan sleeps with?

*How did my sister say that Julia Roberts thinks that Eric solves?

*What does she like the possibility that Susan dances?

*What do they not believe the rumour that he will buy?

*Where do they have a window that opens?

*What did Elnar meet someone who likes?

*What does Susan believe the claim that he robbed yesterday?

*Who doesn't Sam believe the rumour that Sam is dating?

*What did he hear that he believes that he will buy?

*What did they rob someone who bought yesterday?

*What do they whisper the extravagant claim that the blue trumpet likes?

*What does the expensive gift believe that Mary fluently speaks?

*How many blue guitars does the scandalous teddy bear have agents who live in?

*What does the second problem believe the announcement that the Fourier analysis hires?

*What don't the unrealistic Sandman comics quip the plan that the difficult English test likes?

*Who did my likely trumpet say that the crafty party is the only place that knows?

*What does the pregnant girl like the pretty agent that Julia Roberts sings?

*What does the silly car believe the experience that the yellow trumpet did?

*Where does the discreet boat have a funny ring that sings?

*How many cups of coffee does the fair teacher have sleepy hats that direct in?

A.9 Bridge verb island stimuli

A.9.1 Adaptation set

How does she think that he died?

How did she know that he had died?

How does he claim that he got a perfect score on the test?

How did my sister hear that Alex says that he is tired today?

How does she know that she is pregnant?

How does someone who speaks a Balkan language believe that this is easy?

How did he say that today is his last day?

Where does Alex think that Bill fell asleep?

Where did Alex hear that Bill fell asleep?

How does Susan know that the sign pointed us in the right direction?

How does he know that he bought a boat yesterday?

How does Will claim that he solves by Fourier analysis?

How does Sam believe that he is dating someone?

How did he know that he got a perfect score on the test?

How does Susan think that she met someone who robbed a candy store yesterday?

A.9.2 Test set

How did Bill claim that today is his last day?

How does Elnar claim that he has a boat and a car?

How did she think that she bought beans and broccoli?

How does Alex claim that he can make tiramisu and espresso?

How does she know that she failed the test?

How did he say that he went to school?

How does Will think that Bill is pregnant in class?

How did Sam claim that he fell asleep in class today?

How does someone who speaks a Balkan language solve by Fourier analysis?

How does Susan claim that she sleeps with a teddy bear?

How does someone who speaks a Balkan language know beans and broccoli?

How does Elnar hear tiramisu and espresso?

How does Elnar believe tiramisu and espresso?

How did she know that he bought a boat yesterday?

How did Alex claim that he got a perfect score on the test?

How does the discreet party think that the blue trumpet met someone who circulated a teddy bear?

How did Mary think that the movie is directed by Fourier analysis?

How does the open window claim that it has a ring and a salad?

How did the circulating rumour claim an experience that she bought a cup of coffee?

How does Mary claim that she can buy a story and possibilities?

How does the wonder know that it asked for an announced plan?

How did the extravagant gift claim that it went to the sleepy Christmas store?

How does the scandalous phone think that the new girl is discreet in school?

How did the funny bean think that it went home today?

How does someone who eats a silly phone wonder by Broadway?

A.10 Statistical Analyses of Results

Throughout this paper, we compared within-class adaptation effects to cross-class adaptation effects. In this section, we describe how the classes were defined for each analysis and give the two sample t-test reports for each analysis.

A.10.1 Priming Filler-Gap Existence

In Section 7.2, we found that filler-gap existence primed subsequent filler-gap existence across acceptability categories significantly more than shuffled sentences within an acceptability category. Acceptable sentences were defined as: the full sets of object extractions and bridge verb extractions, as well as d-linked left-branch extractions and across-the-board coordinate structure extractions. The rest of the sentences were defined as unacceptable. For processing simplicity, we adapted the models to full construction sets, so *acceptable adapted* models were adapted to either the object extraction set or the bridge verb extraction set. For *acceptable testing*, we included acceptable items from any construction set.

Acceptable adapted

$$\mu_{\text{shuffled}} = 0.64 \quad \mu_{\text{unacceptable}} = 1.32 \\ |t| = 14.5 \quad p < 2.2e^{-16}$$

Unacceptable adapted

$$\mu_{\text{shuffled}} = 0.60 \quad \mu_{\text{acceptable}} = 1.58 \\ |t| = 34.0 \quad p < 2.2e^{-16}$$

To ensure that this testing setup didn't drive our results, we also reran the analysis after classifying all left-branch and coordinate structure items as acceptable for both adaptation and testing, which produced very similar results.

A.10.2 Priming Filler-Gap Constraints

In Section 8.2, we conducted two types of analyses, which we label Baseline and Directional. In Base-

line analyses, we compared matched adherence priming (adherence on adherence and violation on violation) to the lower-bound baseline of adapting to unrelated filler-gap sentences. In the Directional analyses, we compared matched adherence priming (adherence on adherence and violation on violation) to mismatched adherence priming (adherence on violation and violation on adherence).

Subjacency Baseline Analysis

$$\mu_{\text{baseline}} = 1.51 \quad \mu_{\text{matched}} = 1.33 \\ |t| = 4.64 \quad p = 3.6e^{-6}$$

D-Linking Baseline Analysis

$$\mu_{\text{baseline}} = 1.64 \quad \mu_{\text{matched}} = 1.80 \\ |t| = 2.87 \quad p = 0.004$$

ECP Baseline Analysis

$$\mu_{\text{baseline}} = 1.21 \quad \mu_{\text{matched}} = 1.52 \\ |t| = 5.86 \quad p = 6.8e^{-9}$$

ECP Directional Analysis

$$\mu_{\text{mismatched}} = 1.75 \quad \mu_{\text{matched}} = 1.52 \\ |t| = 3.93 \quad p = 9.0e^{-5}$$

L-Marking Baseline Analysis

$$\mu_{\text{baseline}} = 1.21 \quad \mu_{\text{matched}} = 1.27 \\ |t| = 1.01 \quad p = 0.31$$

L-Marking Directional Analysis

$$\mu_{\text{mismatched}} = 1.76 \quad \mu_{\text{matched}} = 1.27 \\ |t| = 7.39 \quad p = 4.6e^{-13}$$